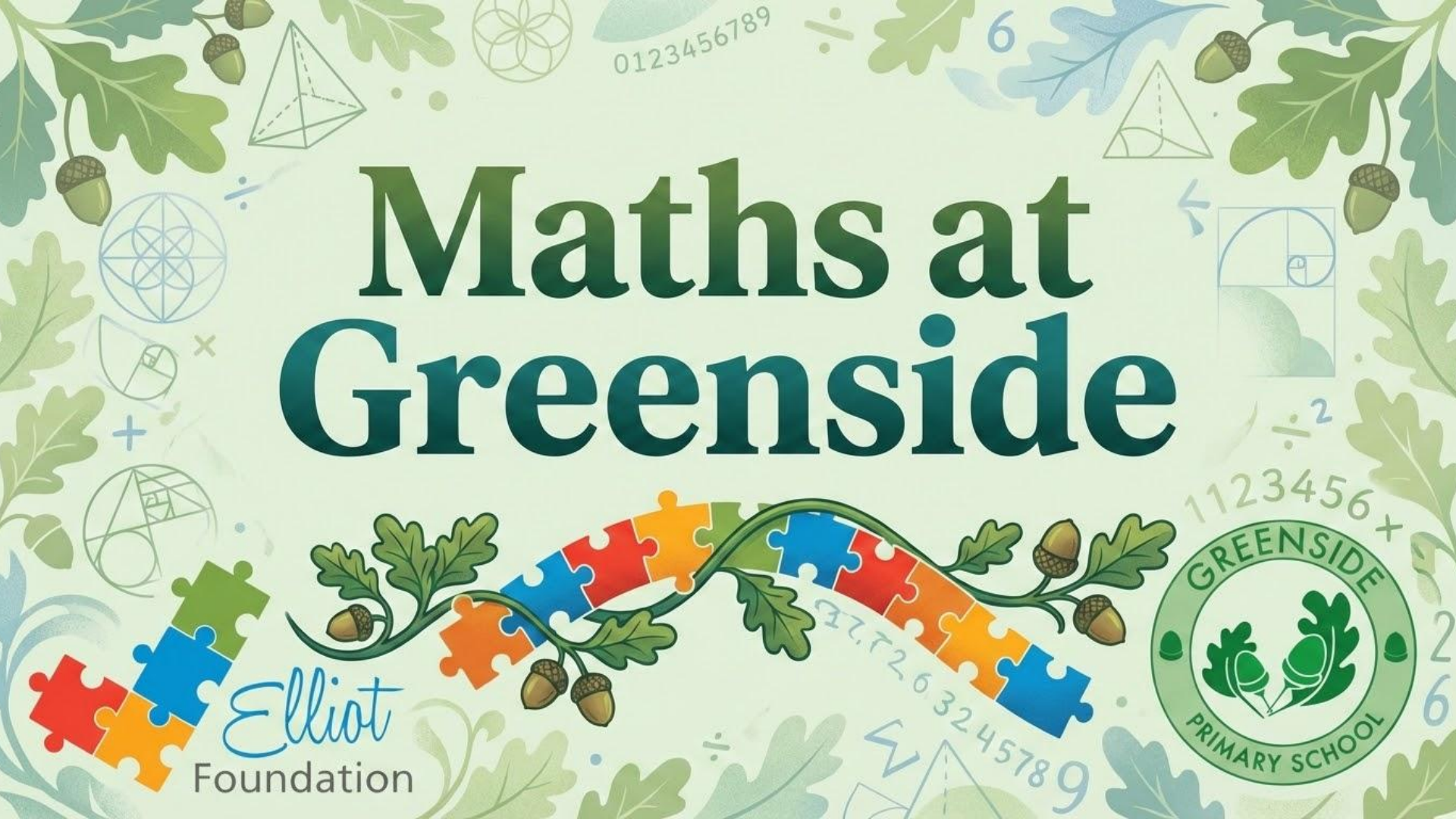


Maths at Greenside



Approach and Vision

At Greenside, we value mathematics and are committed to nurturing, inspiring, and challenging our children.

We use a blend of White Rose and NCETM resources, delivered through the Maths Mastery approach.



Elliot
Foundation



5 Big Ideas in Mastery


$$3 + 5 = \frac{1}{10}$$

$$\alpha = \frac{3}{10}$$

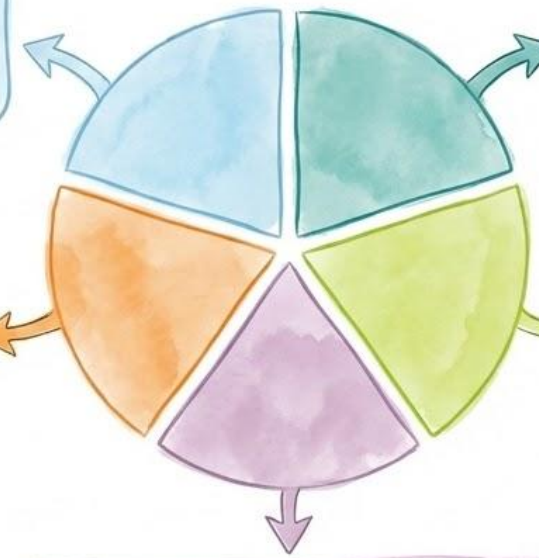


1. Coherence 

2. Representation and Structure 

3. Mathematical Thinking 

4. Fluency 

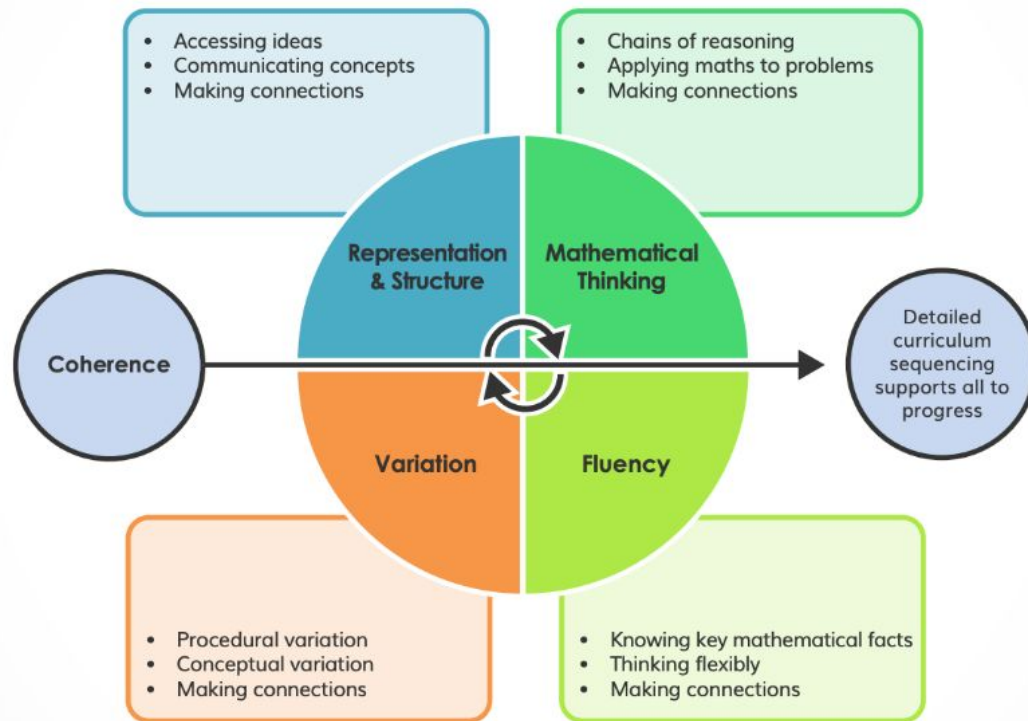


5. Variation 



Teaching for Mastery

Five Big Ideas



Coherence in relation to Maths

Concept:

Coherence strongly links to variation, where learning is built in small but connected steps within a lesson, across lessons, and across years.

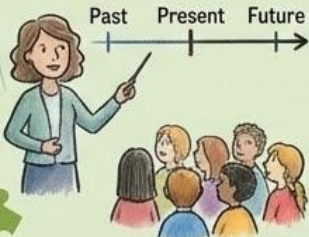
Sequence:

It's not about one task that will support children's learning, but considering the sequence of tasks and the links that are made over time.

Teaching Practice:

I often model a lesson... but I always urge them not to [just teach it]. We need to consider what comes before and have an eye on what is coming next.

Goal: Coherence is all about how the learning builds in ways that make sense to children.



Representation and Structure

Revealing the Structure: The Additive Relationship (Part-Part-Whole)

$$3 + 5 = \frac{1}{10}$$

$$x = \frac{3}{10}$$

$$x = \frac{3}{10}$$



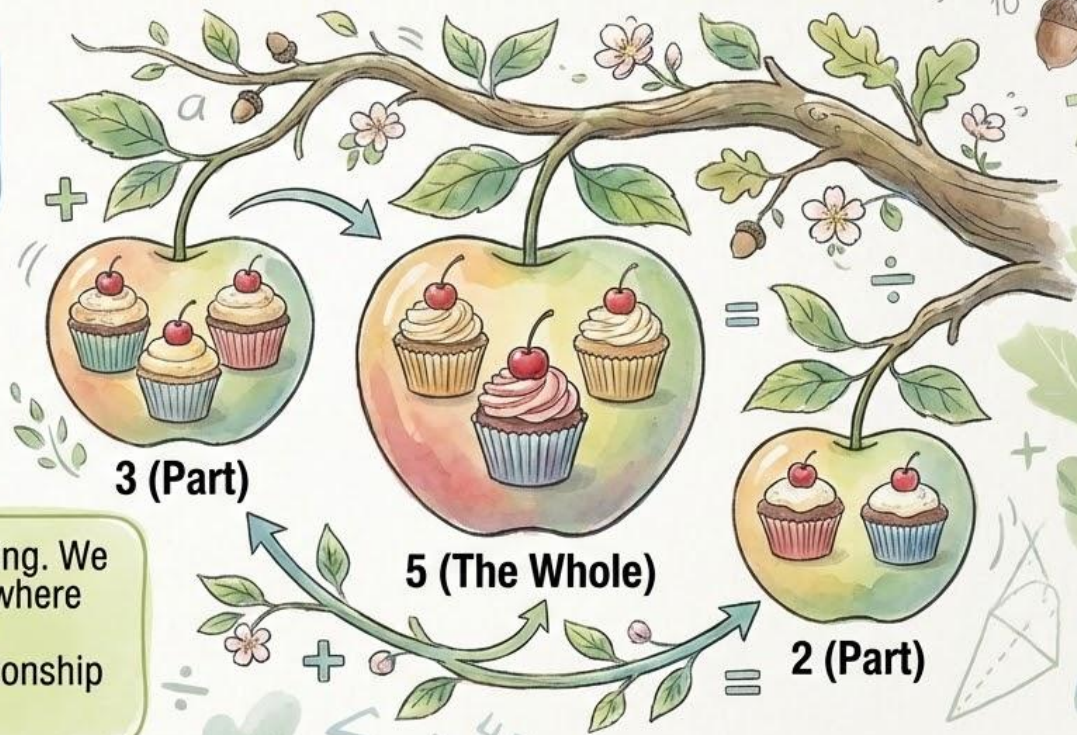
When we represent, we reveal the structure – how and why the maths works. It's about relationships, like putting quantities together.



Example: 3 cakes + 2 cakes = a larger group of 5 cakes. This is an additive structure, often shown as a 'cherry model'.



The model shows partitioning. We don't show all cakes everywhere (not $3+2+5=10!$). Dynamic movement shows the relationship between parts and whole.



5 Alternative Part-Part-Whole Structures

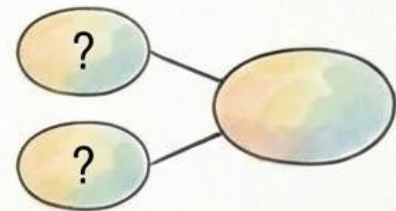
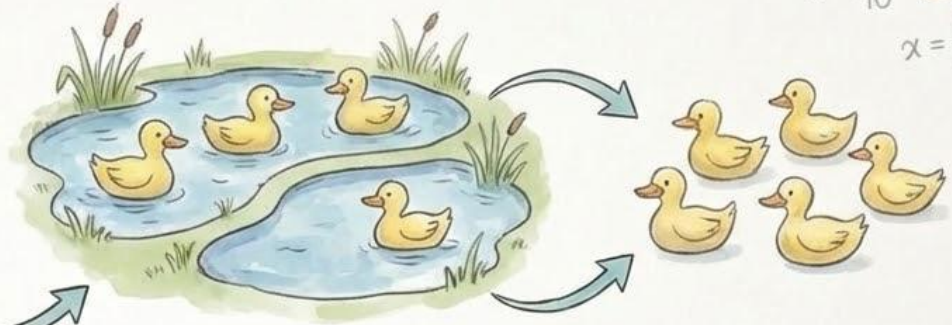
$$3 + 5 = \frac{1}{10}$$

$$x = \frac{3}{10}$$

$$x = \frac{3}{10}$$

That's not the only structure we use to represent the part-part-whole relationship.

At early stages, we use real contexts, like five ducks deciding which of two ponds to swim in, before formalising it into an abstract cherry model.



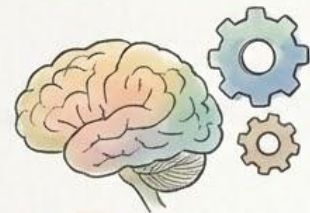
Abstract Cherry Model
(Partitioning)

Bar models are another great tool to draw attention to the equivalence between the parts and the whole. Teachers should select different models to draw out certain aspects of a concept.



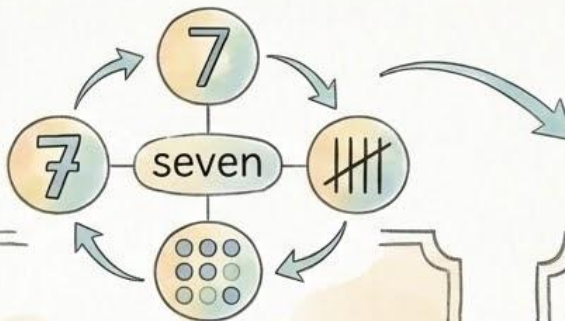
Bar Model (Equivalence)

Developing Mathematical Thinking through Variation



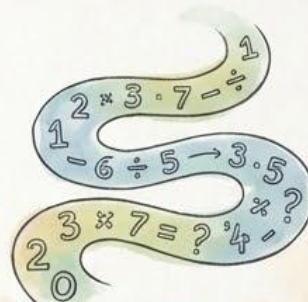
Stimulate Thinking & Reasoning:

The main aim is to stimulate children's mathematical thinking and reasoning.



Link to Variation:

Represent a concept in different ways to draw out essential structures. Carefully select and order representations to build concepts.

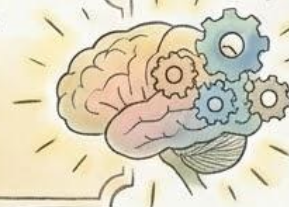


Develop Fluency:

Fluency develops in the movement between representations and the ability to see the structure of the maths in different ways.

Mathematical Thinking


Mathematical thinking lies at the heart of learning mathematics. It is not a separate topic, but the foundation through which we understand and explore concepts. At its core, it is about **identifying relationships and reasoning about them**. Unlike rules to memorise, mathematical relationships are built on **patterns** and **structures** that we can teach pupils to make sense of.



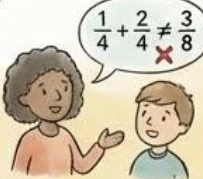
$$3 + 5 = \frac{1}{10}$$

$$x = \frac{3}{10}$$


$$x = \frac{3}{10}$$




Describing
articulating observations



Explaining
why an answer is incorrect?




Conjecturing
making predictions and exploring possibilities



Generalising
identifying patterns and forming broader rules



Justifying
providing logical reasoning to support an answer



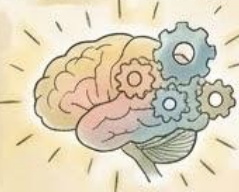
Proving
demonstrating why the maths works through clear reasoning

Fluency

$$3 + 5 = \frac{1}{10}$$

$$x = \frac{3}{10}$$

$$x = \frac{3}{10}$$



Fluency in maths is often misunderstood as simply recalling facts quickly, but it encompasses much more. There are three key elements to fluency:



$$7 \times 8 = 56$$
$$3 + 7 = 10$$

1. Recall and automaticity:

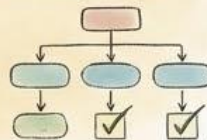
the effortless recall of facts, such as number bonds within 10 and times tables facts, and understanding the relationship between these facts.



2. Procedural fluency:

being confident and accurate with using procedures and being able to select the most appropriate method for the task at hand.

$$124 \times 3 = ?$$
$$\begin{array}{r} 124 \\ \times 3 \\ \hline 100 \end{array}$$



$$\frac{1}{4}$$



3. Flexibility and adaptability:

the skill of moving between different contexts and recognising connections between them. For example, understanding the concept of $\frac{1}{4}$ in various situations, whether it's a fraction of a shape, a portion of time or a proportion of set of objects.

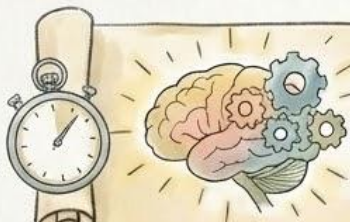
5

Here is a question from the 2024 Year 6 SATs paper:

$$3 + 5 = \frac{1}{10}$$

$$x = \frac{3}{10}$$

$$x = \frac{3}{10}$$



It is likely that some pupils went straight to dividing both numbers by 2, 3, 4, 8 and 9, which would take a very long time. However, if pupils have developed factual fluency, it becomes a very easy question.

Applying Factual Fluency & Divisibility Rules:

2

Tick 2: Both numbers are even (54, 72).

3

$$5 + 4 = 9$$

$$7 + 2 = 9$$

Tick 3: Digits add to a multiple of 3.

4

$$\frac{72}{2} = 36$$

(even)

Tick 4: Half of an even number is even, so it is a multiple of 4.

8 & 9

1 × 0 = 0 × 1
2 × 0 = 0 × 2
3 × 0 = 0 × 3
4 × 0 = 0 × 4
5 × 0 = 0 × 5
6 × 0 = 0 × 6
7 × 0 = 0 × 7
8 × 0 = 0 × 8
9 × 0 = 0 × 9

Tick 8 & 9: Within times tables facts, learned to automaticity ($8 \times 9 = 72$, $6 \times 9 = 54$).

Tick the numbers that are factors of both 54 and 72

2



3



4



8

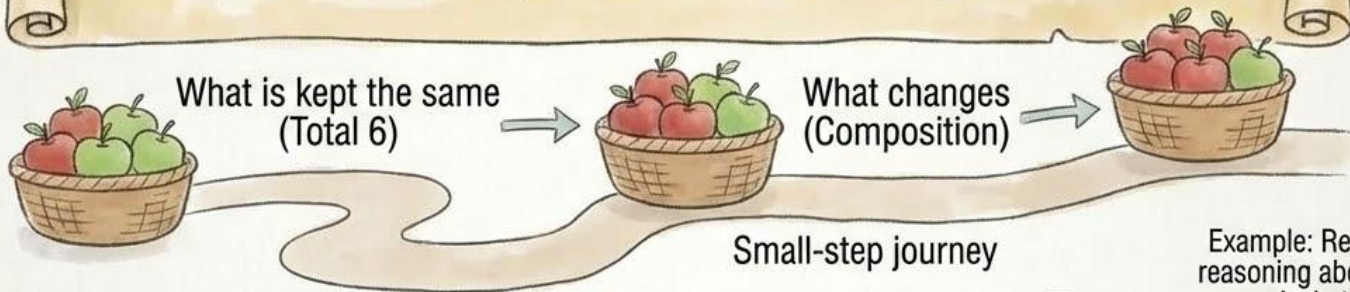


9



Variation

Variation draws attention to essential structures and relationships. It is a carefully constructed small-step journey, considering what is kept the same and what changes.



Example: Reception class reasoning about what is six and what is not six.

Variation includes considering what the concept is, and what it is not. This contrast deepens learning.

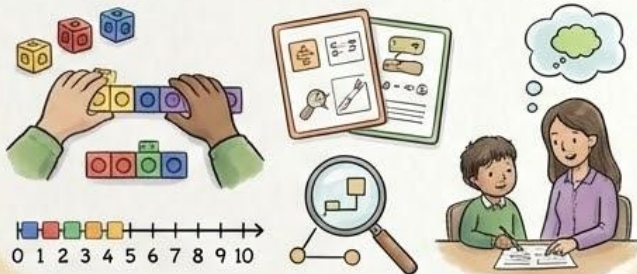


‘How did you know?’



Supporting students with SEN and Higher Attainers

SEN Support: Small steps, visual aids, and guided practice



Concepts are broken down, allowing for extended time and personalized guidance to build confidence.



At Greenside, we ensure every child can thrive in maths.

Higher Attainers: Deeper reasoning, problem-solving, and exploration



Opportunities to explore concepts in greater depth, so all students can progress and succeed at their own level.

EYFS at Greenside

Reception & Nursery Inputs

Reception



DAILY
Maths Inputs

Daily teacher-led maths inputs in Reception;

Nursery



3-4 TIMES/WEEK
Maths Inputs

3-4 times per week in Nursery.

Maths Provision & Outdoor Learning



Dedicated maths areas indoors, with targeted opportunities outdoors.

Explore → Practise → Apply



Continuous Provision: Environment planned for independent exploration, practice, and application of skills.

Nursery Focus: Consolidating Learning



DAILY REVIEW



Daily review and nursery rhymes support number, pattern, and language.

Adult-Directed Activities



2x WEEK
Maths/Phonics

Two adult-directed maths/phonics activities weekly, plus daily art activity.



DAILY
Art Activity

Medium Term Planning/White Rose Overviews:

This is a year 3 example:

	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12
Autumn	Number Place value FREE TRIAL VIEW			Number Addition and subtraction VIEW				Number Multiplication and division A VIEW				
Spring	Number Multiplication and division B VIEW			Measurement Length and perimeter VIEW		Number Fractions A VIEW		Measurement Mass and capacity VIEW				
Summer	Number Fractions B VIEW		Measurement Money VIEW		Measurement Time VIEW		Geometry Shape VIEW		Statistics VIEW		Consolidation	

KS1 and KS2 Planning and Implementation

For KS1 and KS2, teachers plan lessons according to a structured format that reflects the stages of mathematical progression. These stages may take different forms: some are practical, while others focus on written work in groups or individually.

Stage 1 – Practise (Fluency)

The intention is to support students in learning and practising a skill or concept.

Example:
 $6 \times 7 = ?$

Stage 2 – Apply

The intention is for students to apply the skill in new but familiar contexts.

Example: How many wheels are there on 6 bicycles?

Stage 3 – Reasoning / Problem Solving

The intention is for students to explain, justify, and explore mathematical relationships. Students are encouraged to show reasoning about why a method works, not just how.

Example: "Convince me..." or "Which is the odd one out?"

Stage 4 – Deepening Understanding (Mastery with Greater Depth)

The intention is to extend learning beyond the expected level through deep, connected thinking. Students aim to demonstrate rich conceptual understanding that can be applied flexibly in unfamiliar contexts.

Example: Create your own problem; explore "what if..."

Here is an example from students' workbooks, showcasing Year 6 evidence of their learning.

Practising the skill/concept.

To solve a variety of math problems using my fluency, reasoning + problem solving skills.

Practise:
Fractions

- Simplify:
a) $18/24$ b) $45/60$ c) $56/72$
- Find: a) $\%$ of 54 b) $\%$ of 81 c) $1\frac{1}{4} + \frac{1}{2}$

Place Value

- Write 3 950 207 in words.
- Divide by 10, 100, 1,000:
a) $48\ 560 \div 10$ b) $48\ 560 \div 100$ c) $48\ 560 \div 1\ 000$
- What is the value of the 7 in 5 074 321?

Multiplication & Division

- 348×24
- 3.6×12
- $4\ 560 \div 16$
- $63\ 000 \div 90$

Apply:
Questions combining skills or requiring application.

- A box contains $2\frac{1}{4}$ kg of sand. How much is in 7 boxes?
- A rope is 45m long. Zara cuts off $\frac{1}{3}$ of it. How much rope is left?
- A school orders 845 pencils. They are packed in boxes of 24.
How many full boxes can they make, and how many pencils remain?
- A shop sells water at £1.25 each. Calculate the cost of 36 bottles.
- A container holds 3.5 litres. How many containers are needed for 84 litres?

Handwritten solutions:

Fractions:
 $1) \frac{18}{24} = \frac{3}{4}$ $2) \frac{45}{60} = \frac{3}{4}$
 $3) \frac{56}{72} = \frac{7}{9}$ $4) 1\frac{1}{4} + \frac{1}{2} = 1\frac{3}{4}$

Place value:
1) Three million nine hundred and fifty thousand two hundred and seven.
2) a) $48\ 560 \div 10 = 4\ 856$
b) $48\ 560 \div 100 = 485.6$
c) $48\ 560 \div 1\ 000 = 48.56$
3) The value of the 7 is 700.

Multiplication & Division:
1) $348 \times 24 = 8\ 352$
2) $3.6 \times 12 = 43.2$
3) $4\ 560 \div 16 = 285$
4) $63\ 000 \div 90 = 700$

Apply:
1) $2\frac{1}{4} \times 7 = 17\frac{1}{2}$ kg
2) $45 \times \frac{2}{3} = 30$ m
3) $845 \div 24 = 35$ boxes, 5 pencils remain
4) $1.25 \times 36 = 45$ £
5) $84 \div 3.5 = 24$ containers

Apply the skill in a new but familiar concept.

Reasoning:

1. Always, sometimes, never?

Multiplying a number by a fraction less than 1 makes it smaller.
Explain with examples.

Always
 $\frac{1}{2}$ of 10 = 5 $\frac{2}{3}$ of 9 = 6

2. True or false?

$0.4 \times 100 = 4000$
Explain your reasoning.

False because he thought it was 40 and the answer is 40.

3. A pupil says:

"When you divide a number by 10, the digits always move to the right."
Are they correct? Explain with examples including decimals.

Correct: $0.4 = 10 = 0.04$

4. Which is larger:

$\frac{7}{8}$ or 0.82 ?
Prove it using two different methods.

$\frac{82}{100} = \frac{41}{50} = \frac{7}{8}$ $\frac{41}{50} = \frac{82}{100}$ $\frac{7}{8} = \frac{87.5}{100}$ $\frac{82}{100} < \frac{87.5}{100}$

5. Spot the mistake:

Amir says: " $3\frac{1}{2} \times 6 = 18$."
Explain the error and correct the calculation.

He multiplied the whole only.
 $3 \frac{1}{2} \times 6 = 21$

Deepening Understanding:

1. Place Value Scaling Investigation

A number is multiplied by 100 and then divided by 20.

Tasks:

- Choose 5 different numbers (including decimals). Perform the operations: $\times 100$ then $\div 20$. Look for a pattern.
- Explain what single operation could replace $\times 100$ then $\div 20$. Prove your answer with an algebraic expression if you can.

$700 \div 20 = 35$

2. Challenge to Prove: "It Always Works!"

A pupil claims:

"If you divide a number by 8 and then multiply the result by 12, it will always be the same as multiplying the original number by 1.5."

Tasks:

- Test it with at least 4 different numbers. Explain if the claim is correct. If it is correct, prove it using algebra or a diagram.
- If not, explain the mistake and give a corrected rule.

$12 \div 8 = 1.5$
 $6 \div 8 = 0.75$
 $4 \div 8 = 0.5$
 $2 \div 8 = 0.25$

All the one-digit numbers will work because if you times by 100 and divide by 20, 100 is a prime factors of 20. The pattern is 5.

$3 \times 1.5 = 4.5$
 $2 \times 1.5 = 3$
 $4 \times 1.5 = 6$

True because $8 \times 1.5 = 12$

Deepening Understanding:

1. The Fraction Machine Challenge

A "Fraction Machine" takes a number, multiplies it by a fraction, and then divides the result by another fraction.

The machine rule is:

$\frac{1}{15} \times \frac{3}{2} = \frac{6}{30}$ Credit Young

Output = $(\text{Input} \times \frac{3}{4}) \div \frac{2}{3}$

$\frac{1}{5} \times \frac{3}{4} = \frac{3}{20}$ $\frac{3}{20} \div \frac{2}{3} = \frac{9}{40}$

Tasks:

- Pick 3 different inputs (one whole number, one decimal, one fraction).
- Calculate the outputs.
- Describe what the machine always seems to do to a number.
- Can you create your own fraction machine rule that makes the input exactly double? Explain how you know.

$1) \frac{6}{4} \times \frac{3}{4} = \frac{18}{16} \times \frac{3}{2} = \frac{27}{8} = \frac{9}{16} \times \frac{3}{4} = \frac{27}{64}$
 $\frac{400}{100} \times \frac{3}{4} = \frac{300}{100} \times \frac{3}{2} = \frac{900}{100} = 9$

2) for a decimal and whole number!

Deepening understanding beyond the expected level through deep, connected thinking.

Justification and method

Timetabling

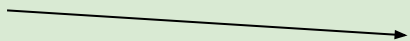
All classes have daily maths lessons, with KS1 and KS2 also participating in additional daily fluency and arithmetic sessions.





Fluency Bee Example

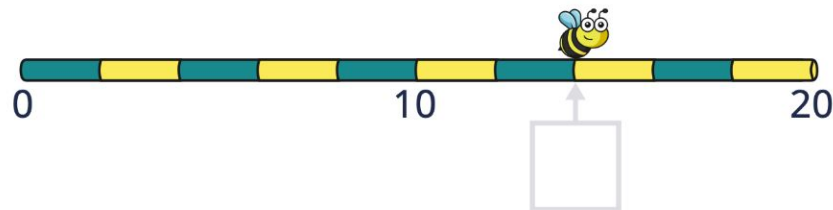
Year 1 example



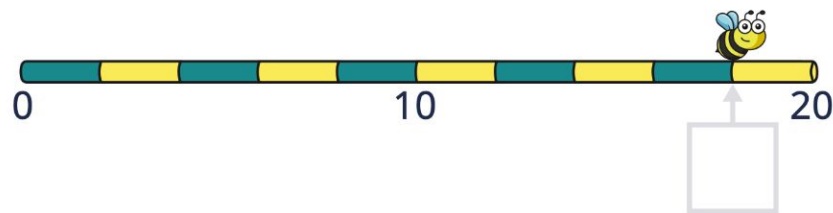
Count in 2s

Where has Bee landed?

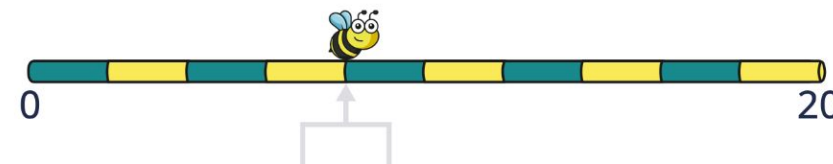
1



2



3



To end on a beautiful note, here are some comments:

